Master Informatics Eng.

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Concepts from undegrad Computer Systems (2)

(some slides are borrowed)

- Algorithm + Data Structures
  - Determines number of operations executed
  - Determines how efficient data is assessed
- Programming language, compiler, architecture
  - Determine number of machine instructions executed per operation
- Processor and memory system
  - Determine how fast instructions are executed
- I/O system (including OS)
  - Determines how fast I/O operations are executed

Response Time and Throughput

- Response time
  - How long it takes to do a task
- Throughput
  - Total work done per unit time
    - e.g., tasks/transactions/… per hour
- How are response time and throughput affected by
  - Replacing the processor with a faster version?
  - Adding more processors?
- We'll focus on response time for now…

CPU Time (single-core)

$$\text{CPU Time} = \text{CPU Clock Cycles} \times \text{Clock Cycle Time}$$

$$= \frac{\text{CPU Clock Cycles}}{\text{Clock Rate}}$$

- Performance improved by
  - Reducing number of clock cycles
  - Increasing clock rate
  - Hardware designer must often trade off clock rate against cycle count

$$\text{Clock Cycles} = \text{Instruction Count} \times \text{Cycles per Instruction}$$

$$\text{CPU Time} = \text{Instruction Count} \times \text{CPI} \times \text{Clock Cycle Time}$$

$$= \frac{\text{Instruction Count} \times \text{CPI}}{\text{Clock Rate}}$$

- Instruction Count, **IC**, for a program
  - Determined by program, ISA and compiler
- Average cycles per instruction (**CPI**)
  - Determined by CPU hardware
  - If different instructions have different CPI
    - Average CPI affected by instruction mix

The BIG Picture

$$\text{CPU Time} = \underbrace{\frac{\text{Instructions}}{\text{Program}}}_{\text{IC}} \times \underbrace{\frac{\text{Clock cycles}}{\text{Instruction}}}_{\text{CPI}} \times \underbrace{\frac{\text{Seconds}}{\text{Clock cycle}}}_{T_c}$$

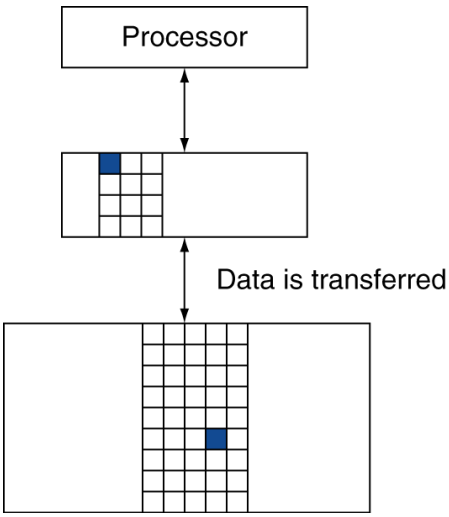
- Performance depends on
  - Algorithm: affects IC, possibly CPI
  - Programming language: affects IC, CPI
  - Compiler: affects IC, CPI
  - Instruction set architecture: affects IC, CPI, T_c
  - Processor design: ILP, memory hierarchy, ...

The BIG Picture

- Pipelining improves performance by increasing instruction throughput
  - Executes multiple instructions in parallel
  - Each instruction has the same latency
- Subject to hazards
  - Structure, data, control
- Instruction set design affects complexity of pipeline implementation

The BIG Picture

- Yes, but not as much as we'd like
- Programs have real dependencies that limit ILP
- Some dependencies are hard to eliminate
  - e.g., pointer aliasing
- Some parallelism is hard to expose
  - Limited window size during instruction issue
- Memory delays and limited bandwidth
  - Hard to keep pipelines full
- Speculation can help if done well



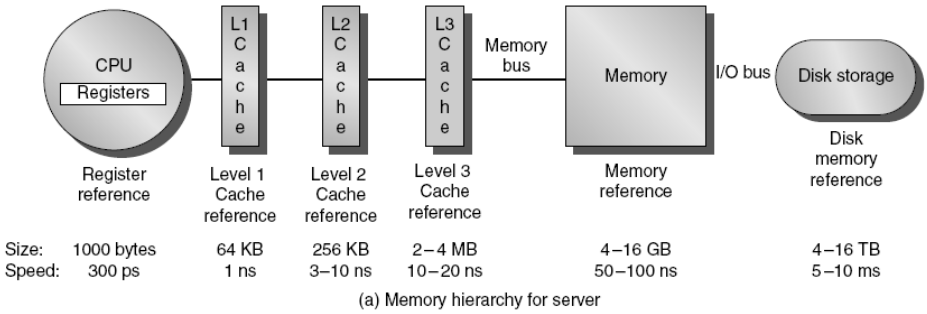
- Block (aka line): unit of copying
  - May be multiple words
- If accessed data is present in upper level
  - Hit: access satisfied by upper level
    - Hit ratio: hits/accesses
- If accessed data is absent
  - Miss: block copied from lower level
    - Time taken: miss penalty
    - Miss ratio: misses/accesses = 1 – hit ratio
  - Then accessed data supplied from lower level

The BIG Picture

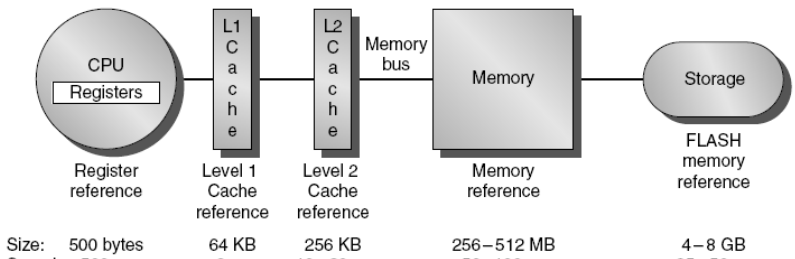
- Common principles apply at all levels of the memory hierarchy
  - Based on notions of caching
- Decisions at each level in the hierarchy
  - Block placement
  - Finding a block
  - Replacement on a miss
  - Write policy

§5.5 A Common Framework for Memory Hierarchies

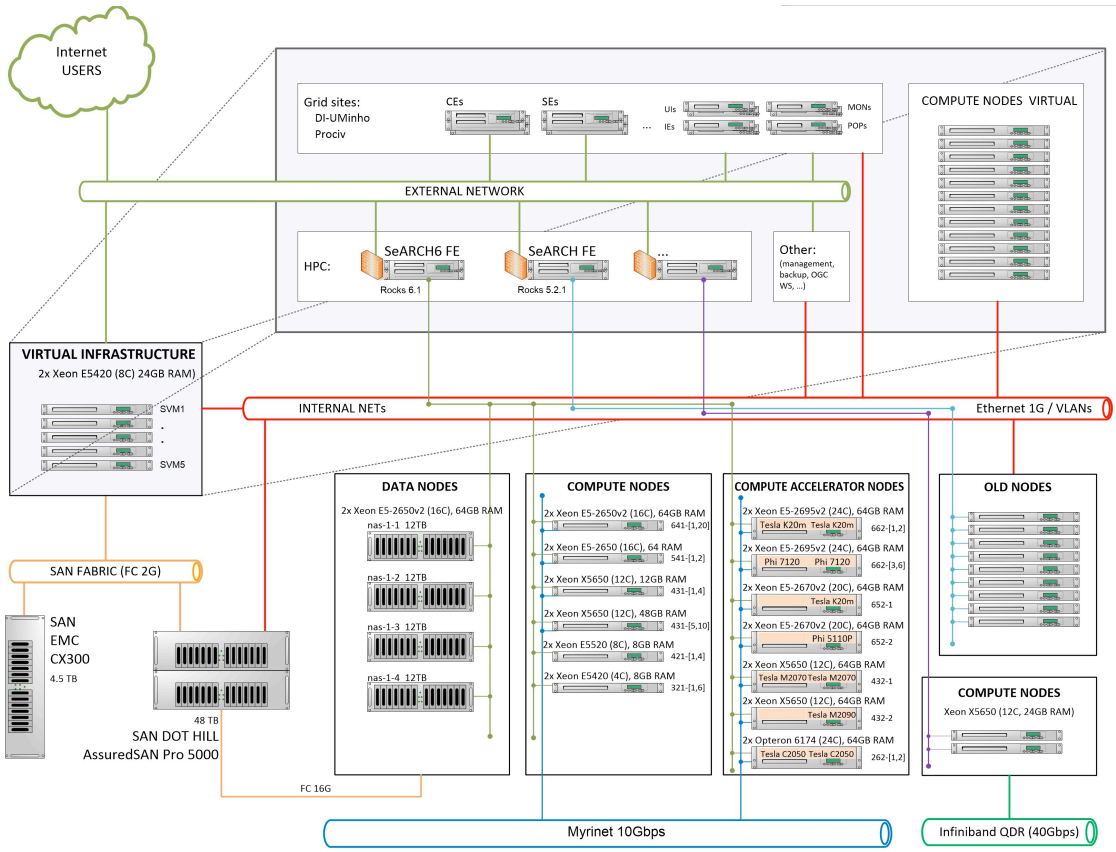
- Primary cache private to CPU/core
  - Small, but fast
- Level-2 cache services misses from primary cache
  - Larger, slower, but still faster than main memory
- High-end systems include L3 cache
- Main memory services L2/3 cache misses



(a) Memory hierarchy for server



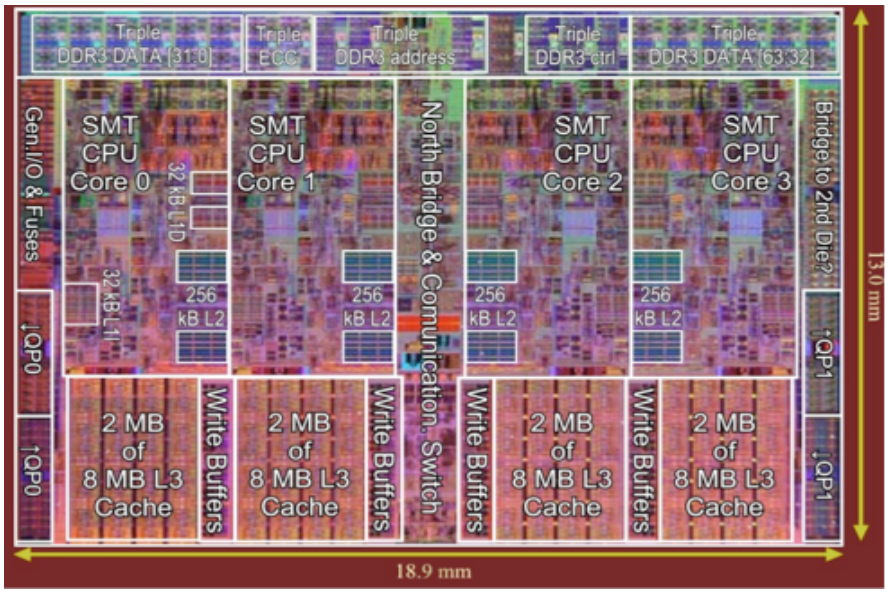
(b) Memory hierarchy for a personal mobile device



segment	rack	rank	queues	properties	dual cpu	clock (GHz)	cores	memory (GB)	accelerator	net
Broadwell	781	1	mogipc,day	r781,m256,d1024	E5-2683v4	2.10	32	256	NA	gbe
		2	biocnat,day	r781,m256,d1024	E5-2683v4	2.10	32	256	NA	gbe
	771	1	biocnat,day	r771,m128,d1024	E5-2660v4	2.00	28	128	NA	gbe
		2	biocnat,day	r771,m128,d1024	E5-2660v4	2.00	28	128	NA	gbe
Ivy Bridge	662	1	mei,day	r662,m64,d80,myri,repler,k20	E5-2695v2	2.40	24	64	2xK20m	gbe/myri
		2	mei,day	r662,m64,d80,myri,repler,k20	E5-2695v2	2.40	24	64	2xK20m	gbe/myri
		...								
		6	mei,day	r662,m64,d80,myri,phi,7120	E5-2695v2	2.40	24	64	2xPhi 7120	gbe/myri
	652	1	mei,day	r652,m64,d80,myri,repler,k20	E5-2670v2	2.50	20	64	Tesla K20m	gbe/myri
		2	mei,day	r652,m64,d80,myri,phi,5110	E5-2670v2	2.50	20	64	Phi 5110P	gbe/myri
	641	1	day,week,month	r641,m64,d190,myri	E5-2650v2	2.60	16	64	NA	gbe/myri
		...								

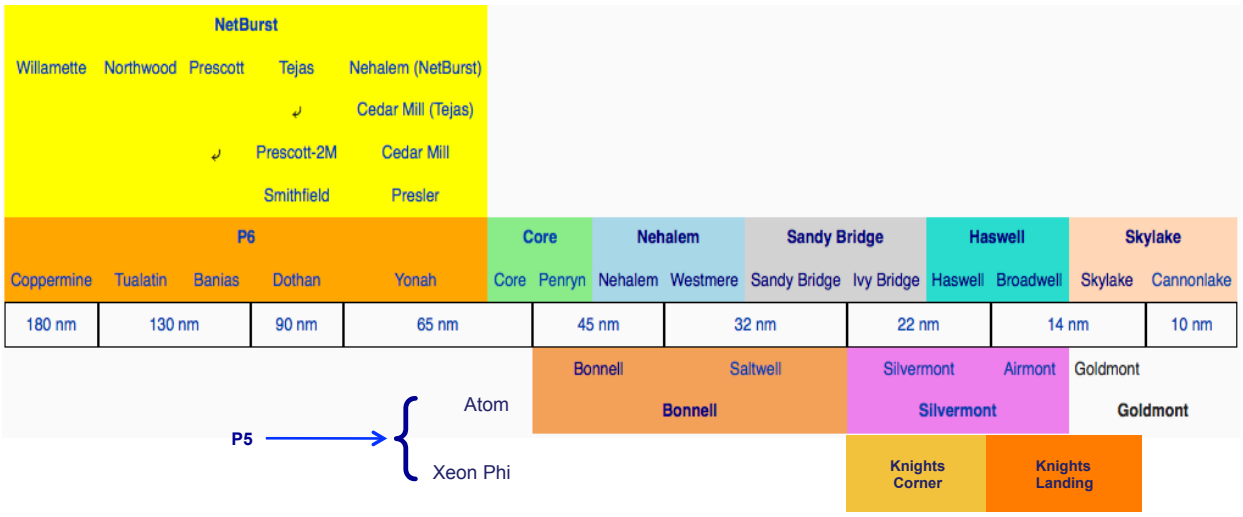
Multilevel On-Chip Caches

Intel Nehalem 4-core processor



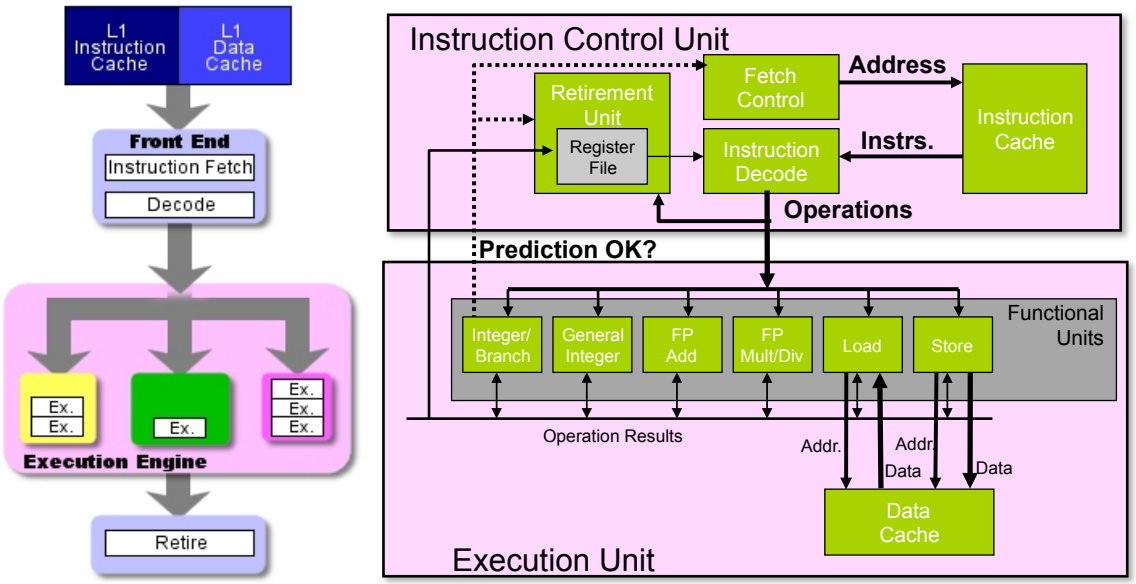
Per core: 32KB L1 I-cache, 32KB L1 D-cache, 512KB L2 cache

Internal x86 roadmap



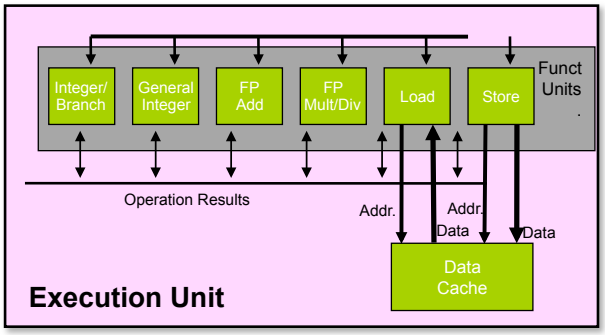
Internal architecture of Intel P6 processors

Note: "Intel P6" is the common μarch name for PentiumPro, Pentium II & Pentium III, which inspired Core, Nehalem and later generations



Some capabilities of Intel P6

- **Parallel execution of several instructions**
  - 2 **integer** (1 can be **branch**)
  - 1 **FP Add**
  - 1 **FP Multiply or Divide**
  - 1 **load**
  - 1 **store**



- Some instructions require > 1 cycle, but can be pipelined:

Instruction	Latency	Cycles/Issue
Load / Store	3	1
Integer Multiply	4	1
Integer Divide	36	36
Double/Single FP Multiply	5	2
Double/Single FP Add	3	1
Double/Single FP Divide	38	38

A detailed example: generic & abstract form of `combine`

```
void abstract_combine4(vec_ptr v, data_t *dest)
{
  int i;
  int length = vec_length(v);
  data_t *data = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP data[i];
  *dest = t;
}
```

- **Procedure to perform addition** (w/ some improvements)
  - compute the sum of all vector elements
  - store the result in a given memory location
  - structure and operations on the vector defined by ADT
- **Metrics**
  - Clock-cycles Per Element, **CPE**

Converting instructions with registers into operations with tags

- **Assembly version for `combine4`**
  - data type: *integer* ; operation: *multiplication*

```
.L24:                           # Loop:
  imull (%eax,%edx,4),%ecx      # t *= data[i]
  incl  %edx                    # i++
  cmpl  %esi,%edx               # i:length
  jl    .L24                    # if < goto Loop
```

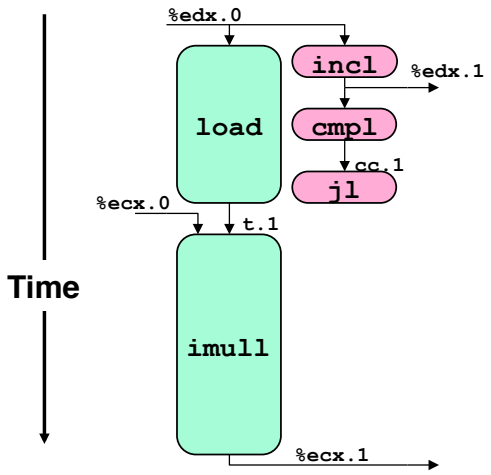
- **Translating 1st iteration**

```
.L24:
  imull (%eax,%edx,4),%ecx

  incl  %edx
  cmpl  %esi,%edx
  jl    .L24
```

```
load  (%eax,%edx.0,4) → t.1
imull t.1, %ecx.0     → %ecx.1
incl  %edx.0          → %edx.1
cmpl  %esi, %edx.1    → cc.1
jl    -taken cc.1
```

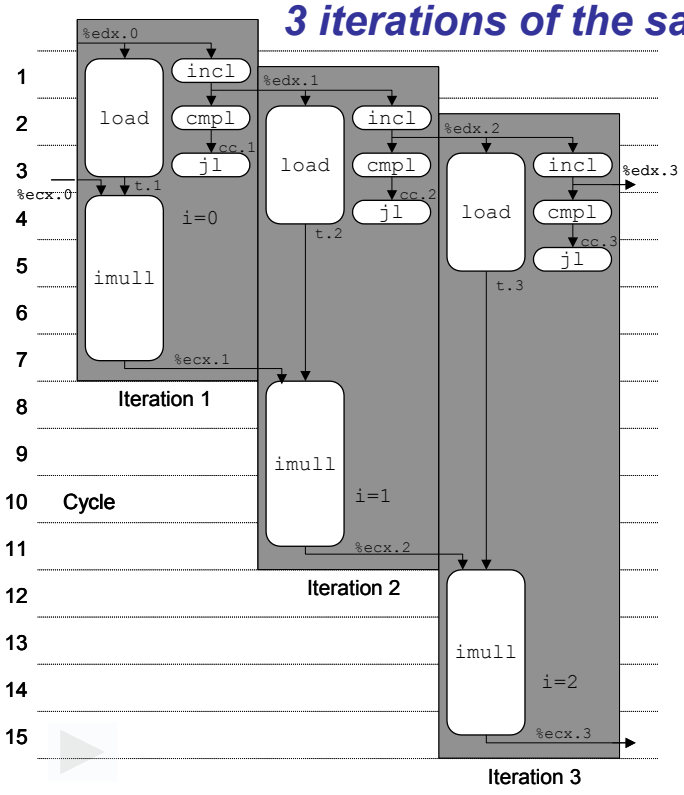
Visualizing instruction execution in P6: 1 iteration of the multiplication cycle on `combine`




```
load   (%eax,%edx.0,4) ➔ t.1
imull  t.1, %ecx.0     ➔ %ecx.1
incl   %edx.0          ➔ %edx.1
cmpl   %esi, %edx.1    ➔ cc.1
jl     -taken cc.1
```

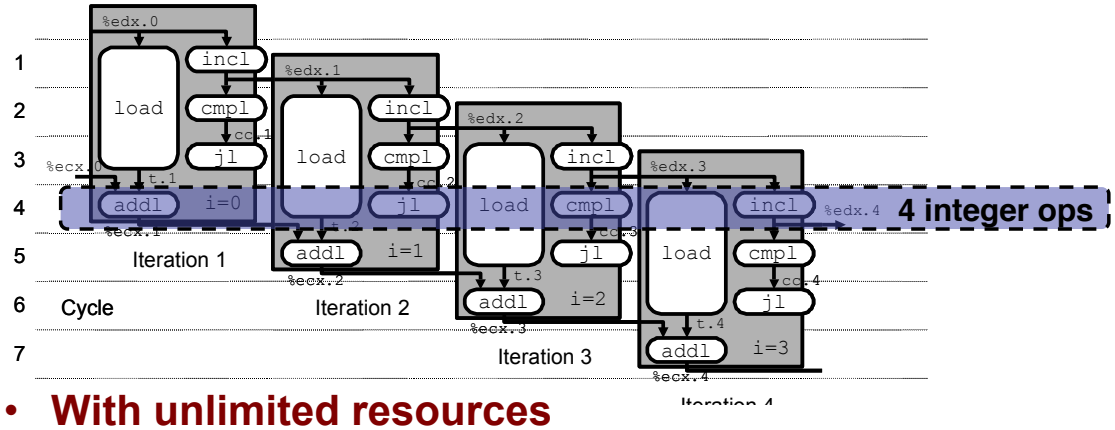
- **Operations**
  - vertical axis shows the time the instruction is executed
    - an operation cannot start with its operands
  - time length measures latency
- **Operands**
  - arcs are only showed for operands that are used in the context of the *execution unit*

Visualizing instruction execution in P6: 3 iterations of the same cycle on `combine`



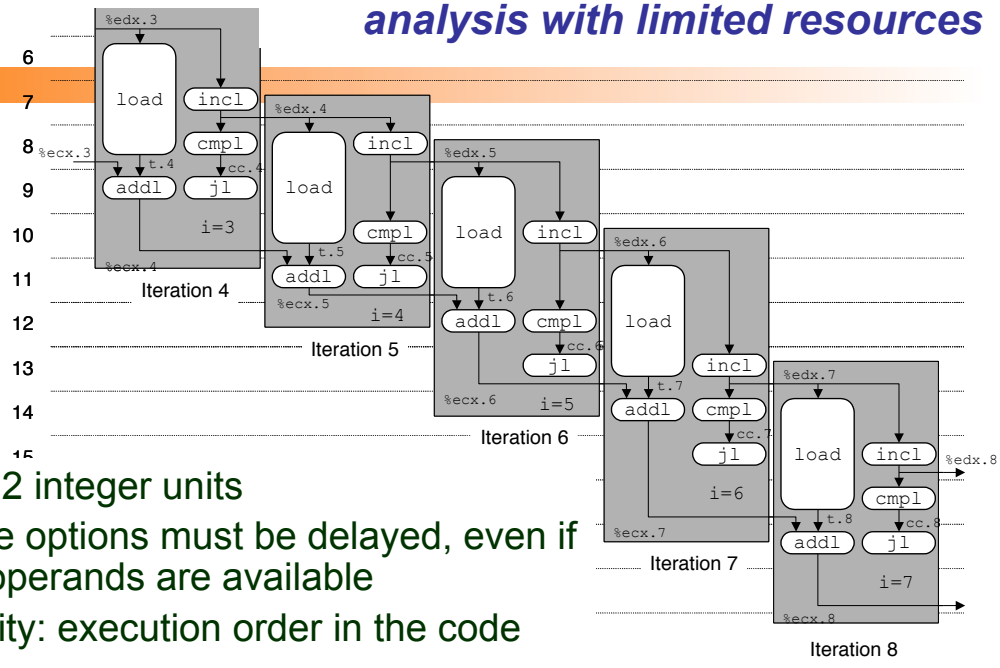
- **With unlimited resources**
  - parallel and pipelined execution of operations at the EU
  - out-of-order and speculative execution
- **Performance**
  - limitative factor: latency of integer multiplication
  - CPE: 4.0

Visualizing instruction execution in P6: 4 iterations of the addition cycle on `combine`



- **With unlimited resources**
- **Performance**
  - it can start a new iteration at each clock cycle
  - theoretical CPE: 1.0
  - it requires parallel execution of 4 integer operations

Iterations of the addition cycles: analysis with limited resources



- only 2 integer units
- some options must be delayed, even if the operands are available
- priority: execution order in the code

- **Performance**
  - expected CPE: 2.0

Machine dependent optimization techniques: loop unroll (1)

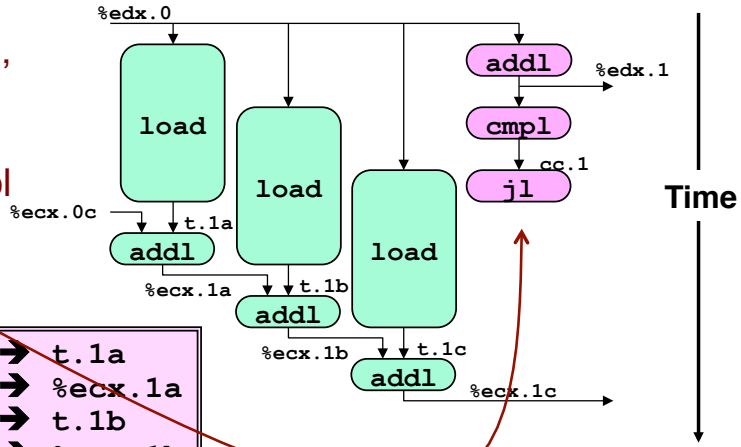
```
void combine5(vec_ptr v, int *dest)
{
  int length = vec_length(v);
  int limit = length-2;
  int *data = get_vec_start(v);
  int sum = 0;
  int i;
  /* junta 3 elem's no mesmo ciclo */
  for (i = 0; i < limit; i+=3) {
    sum += data[i] + data[i+1]
           + data[i+2];
  }
  /* completa os restantes elem's */
  for (; i < length; i++) {
    sum += data[i];
  }
  *dest = sum;
}
```

Optimization 4:

- merges several (**3**) iterations in a single loop cycle
- reduces cycle overhead in loop iterations
- runs the extra work at the end
- **CPE: 1.33**

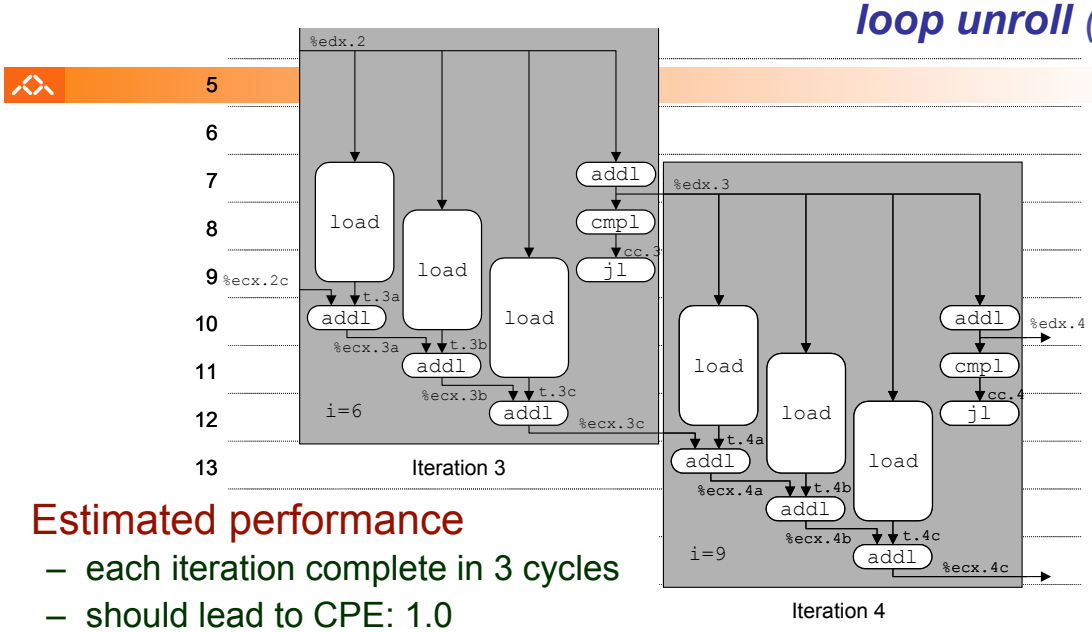
Machine dependent optimization techniques: loop unroll (2)

- **loads** can be pipelined, there are no dependencies
- only a set of loop control instructions




```
load (%eax,%edx.0,4)   → t.1a
iaddl t.1a, %ecx.0c    → %ecx.1a
load 4(%eax,%edx.0,4)  → t.1b
iaddl t.1b, %ecx.1a    → %ecx.1b
load 8(%eax,%edx.0,4)  → t.1c
iaddl t.1c, %ecx.1b    → %ecx.1c
iaddl $3,%edx.0        → %edx.1
cmpl %esi, %edx.1      → cc.1
jl-taken cc.1
```

Machine dependent optimization techniques: loop unroll (3)



- Estimated performance
  - each iteration complete in 3 cycles
  - should lead to CPE: 1.0
- Measured performance
  - CPE: 1.33
  - 1 iteration for each 4 cycles

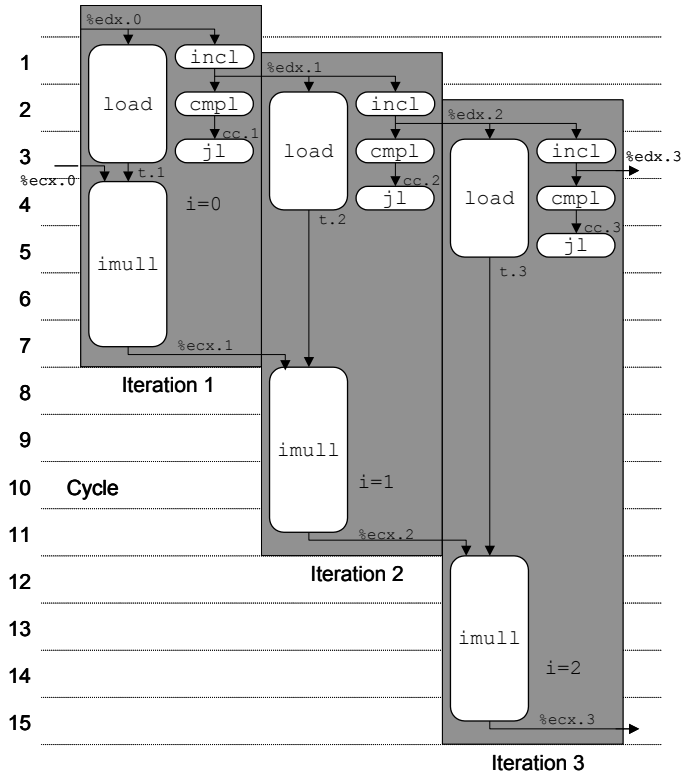
Machine dependent optimization techniques: loop unroll (4)

CPE value for several cases of loop unroll:

Degree of Unroll		1	2	3	4	8	16
Integer	Addition	2.00	1.50	1.33	1.50	1.25	1.06
Integer	Product	4.00					
fp	Addition	3.00					
fp	Product	5.00					

- only improves the integer addition
  - remaining cases are limited to the unit latency
- result does not linearly improve with the degree of unroll
  - subtle effects determine the exact allocation of operations

What else can be done?



Machine dependent optimization techniques: loop unroll with parallelism (1)

Sequential ... *versus* parallel!

```
void combine6(vec_ptr v, int *dest)
{
  int length = vec_length(v);
  int limit = length-1;
  int *data = get_vec_start(v);
  int x0 = 1;
  int x1 = 1;
  int i;
  /* junta 2 elem's de cada vez */
  for (i = 0; i < limit; i+=2) {
    x0 *= data[i];
    x1 *= data[i+1];
  }
  /* completa os restantes elem's */
  for (; i < length; i++) {
    x0 *= data[i];
  }
  *dest = x0 * x1;
}
```

Optimization 5:

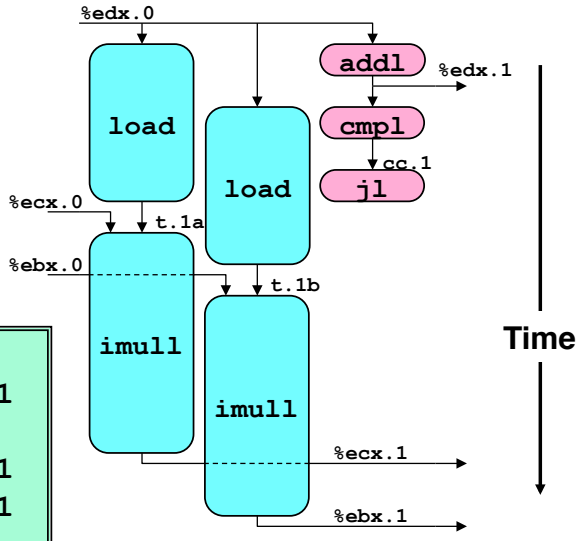
- accumulate in 2 different products
  - can be in parallel, if OP is associative!
- merge at the end

– Performance

- **CPE: 2.0**
- improvement 2x

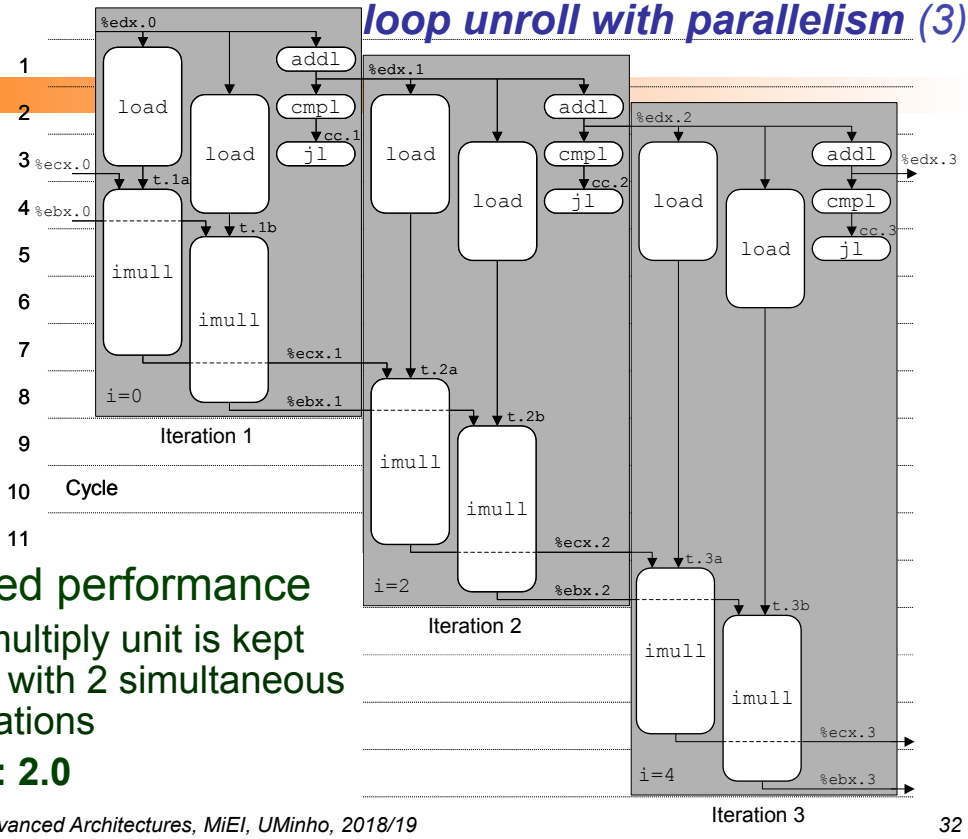
Machine dependent optimization techniques: loop unroll with parallelism (2)

- each product at the inner cycle does not depend from the other one…
- so, they can be pipelined
- known as iteration splitting




```
load (%eax,%edx.0,4)   ➔ t.1a
imull t.1a, %ecx.0     ➔ %ecx.1
load 4(%eax,%edx.0,4)  ➔ t.1b
imull t.1b, %ebx.0     ➔ %ebx.1
iaddl $2,%edx.0        ➔ %edx.1
cmpl %esi, %edx.1      ➔ cc.1
jl-taken cc.1
```


Machine dependent optimization techniques: loop unroll with parallelism (3)



Estimated performance

- the multiply unit is kept busy with 2 simultaneous operations
- **CPE: 2.0**

Code optimization techniques: comparative analyses of `combine`

Method	Integer		Real (single precision)	
	+	*	+	*
Abstract -g	42.06	41.86	41.44	160.00
Abstract -O2	31.25	33.25	31.25	143.00
Move `vec_length`	20.66	21.25	21.15	135.00
Access to data	6.00	9.00	8.00	117.00
Accum. in temp	2.00	4.00	3.00	5.00
Unroll 4x	1.50	4.00	3.00	5.00
Unroll 16x	1.06	4.00	3.00	5.00
Unroll 2x, paral. 2x	1.50	2.00	2.00	2.50
Unroll 4x, paral. 4x	1.50	2.00	1.50	2.50
Unroll 8x, paral. 4x	1.25	1.25	1.50	2.00
Theoretical Optimiz	1.00	1.00	1.00	2.00
Worst : Best	*39.7*	*33.5*	*27.6*	*80.0*

Code optimization: ILP limitations

- It requires a lot of registers!
  - to save results from add/multip
  - only 6 integer registers in IA32
    - also used as pointers, loop control, …
  - 8 fp registers
  - when registers aren't enough, temp's are pushed to the stack
    - cuts performance gains (see assembly in integer product with 8x unroll & 8x parallelism)
  - re-naming registers is not enough
    - it is not possible to reference more operands than those at the instruction set
    - … main drawback at the IA32 instruction set
- Operations to parallelize must be associative!
  - fp add & multipl in a computer is not associative!
    - (3.14+1e20)-1e20 not always the same as 3.14+(1e20-1e20)…

Limitation of parallelism: not enough registers

- **`combine`**
  - integer multiplication
  - 8x unroll & 8x parallelism
  - 7 local variables share 1 register (`%edi`)
    - note the stack accesses
    - performance improvement is compromised...
    - consequence: register spilling

```
.L165:
     imull (%eax),%ecx
     movl -4(%ebp),%edi
     imull 4(%eax),%edi
     movl %edi,-4(%ebp)
     movl -8(%ebp),%edi
     imull 8(%eax),%edi
     movl %edi,-8(%ebp)
     movl -12(%ebp),%edi
     imull 12(%eax),%edi
     movl %edi,-12(%ebp)
     movl -16(%ebp),%edi
     imull 16(%eax),%edi
     movl %edi,-16(%ebp)
   ...
     addl $32,%eax
     addl $8,%edx
     cmpl -32(%ebp),%edx
     jl .L165
```